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Reliability analysis for hydrokinetic turbine blades

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ABSTRACT

Reliability is an important element in the performance of hydrokinetic turbines. It is also a driving factor of the system lifetime cost. In this paper, we perform time-dependent reliability analysis for the blades of a river-based horizontal-axis hydrokinetic turbine. Based on the stochastic representation of the monthly river velocity and material strength, a limit-state function is established with the classical blade element momentum method. In the limit-state function, a failure is defined as the event when the flapwise bending moment exceeds the allowable moment that corresponds to the ultimate strength of the material. The upcrossing rate method is employed to calculate the time-dependent reliability of the hydrokinetic turbine blade over its design life period. The results indicate that setting a proper cut-out river velocity is important for the reliability of the hydrokinetic turbine blade.

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1. Introduction

Hydrokinetic energy refers to energy generated from the ocean wave, current, tidal, and in-stream current energy resources. It has received increasing attention recently [1–7] because it can provide supplies of clean, renewable energy for the world's carbon-free energy demand [3,5]. Several technologies have been developed to extract hydrokinetic energy, such as float or buoy systems and oscillating water column devices. Among these technologies, hydrokinetic turbines are one of the most commonly used, especially in inland rivers. The hydrokinetic turbine technology is still under development and has not been fully commercialized yet. One factor, which plays a vital role in the commercialization, is the reliability of hydrokinetic turbines. The reliability is directly associated with the availability of the hydrokinetic turbine and its energy-cost ratio. It is one of the hydrokinetic turbine.

The Failure Modes and Effect Analysis (FMEA) of wind turbines has shown that the turbine blades have the highest risk priority number [8,9], and the safety of the turbine blade should be given a special consideration during the design of the wind turbine. We expect that it is the same case for a hydrokinetic turbine because it shares similarities with a wind turbine. In addition, for a hydrokinetic turbine, there are uncertainties inherent in the river environment, the stress of the turbine blades, and the resistance of materials. Their impact on the reliability of blades should be evaluated during the blade design.

The technology of the hydrokinetic turbine is still under development, and the research on the reliability of hydrokinetic turbines has rarely been reported. But there are similarities between hydrokinetic turbines and wind turbines. Because the technology of wind turbines is relatively mature, we can therefore use the results of the reliability analysis of wind turbines as a reference for hydrokinetic turbines. The blades of both types of turbines have similar failure modes, such as fatigue and fracture due to ultimate loading. For hydrokinetic turbine blades, however, the natural climates, which govern the loading on the turbine blades, are different from those of wind turbine blades. One of the differences is that the river flow velocity has longer memory than the wind climate. In the past decades, several methods were developed to analyze the reliability of wind turbine blades. For example, Agarwal [10] proposed efficient extrapolation procedures to predict the long-term extreme loads for offshore wind turbines based on limited field data. By using inverse reliability, Saranyasoontorn and Manuel [11,12] studied the reliability of wind turbines against extreme loads. Similarly, Ronold [13] proposed a nested reliability analysis method for analysis of the safety of a wind turbine rotor blade against failure in ultimate loading. However, these reliability analysis methods for wind turbine blades cannot be directly applied to the reliability of hydrokinetic turbine blades because as mentioned above, the wind environment is different from the river environment. Besides, most of the previous research has not considered the time influence on the loading of turbine blades.





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The river loading varies over time, and there is some kind of seasonal characteristic in the monthly river velocity over a long time period. The monthly river velocity, which governs the loading of hydrokinetic turbine blades, is an auto-correlated stochastic process. The reliability of hydrokinetic turbine blades, therefore, also varies over time. Thus time-dependent reliability analysis is necessary for river-based hydrokinetic turbine blades.

The nested reliability method proposed by Ronold [13] can address the time-dependent problem by discretizing the time period into a series of time intervals. But it may not be feasible for the hydrokinetic turbine blade reliability analysis because the monthly river flow velocity has much longer memory than the wind climates [14]. The Monte Carlo simulation (MCS) can be used, but it is computationally expensive.

For general time-dependent reliability analysis, many methods have been proposed in the past decades, including the Gamma distribution method and the Markov method. The most commonly used one is the upcrossing rate method [15–18]. This method is based on the Poisson assumption, and the key of this method is the calculation of the upcrossing rate. In order to increase the accuracy of computation, Sudret [19] proposed an analytical derivation of the upcrossing rate, and this method was used by Zhang and Du [20] later, for reliability analysis of function generator mechanisms over a certain time period. The upcrossing method can also be employed for the time-dependent reliability analysis of hydrokinetic turbine blades.

The purpose of this paper is to develop a time-dependent reliability analysis model for river-based hydrokinetic turbine blades. We consider a horizontal-axis hydrokinetic turbine with three turbine blades. By accounting for the failure due to excessive flapwise bending moment, we compute the reliability of turbine blades over a 20-year design life. The stochastic characteristics of the monthly river velocity are modeled based on the monthly river discharge dataset of the Missouri river and the relationship between the river discharge and river velocity. The flapwise bending moment of the turbine blade is obtained using the classical blade element momentum model. And the upcrossing rate method is employed to carry out the reliability analysis.

In Section 2, we analyze the stochastic characteristics of the river flow velocity. Based on that, we establish a limit-state function using the blade element momentum theory. In Section 3, we explain the time-dependent reliability analysis method for hydro-kinetic turbine blades, and an example is given in Section 4. Conclusions are provided in Section 5.

2. Statement of problem

In this section, we discuss the major factors that affect the reliability of the hydrokinetic turbine blades and then establish a limit-state function for the reliability analysis.

2.1. River flow velocity

2.1.1. River flow velocity formulation

The river flow velocity, which governs the loading of hydrokinetic turbine blades, varies both in space and time. The spacial variations of the river flow velocity are presented as the river velocity profile in the cross section of the river. The river flow velocity also fluctuates randomly over time. The river flow velocity should therefore be described by a time-dependent random filed that varies randomly over space and time. The complicated properties of the river flow velocity, however, have brought great challenges to the measurements of river velocity, especially for large rivers with depths exceeding several meters and with velocities greater than 1m/s [21]. As a result, the information of the spatial variations of the river flow velocity is generally unavailable.

Fortunately, the river discharge data of many rivers are usually recorded and can be used to derive the statistical property of the average river flow velocity over the river cross section. For this reason, in this work, we only account for the average river flow velocity over the river cross section, and we then model the river flow velocity as a stochastic process. In other words, the spatial variation of the river flow velocity over location is neglected, and only its time variation is considered.

The other reasons of using a stochastic process for the river flow velocity are as follows: First, the hydrokinetic turbine system in this study is different from traditional hydropower plants. It is designed to be portable and is installed on a removable device, such as a vessel. This enables the turbine system to operate at different locations (in terms of x-, y-, and z-coordinates). It is difficult to predetermine at which location the velocity should be used. Second, for large rivers, where the hydrokinetic turbine is supposed to operate, the effect of the velocity profile in the cross section is smaller than that of small rivers. Third, the present work concentrates on the general time-dependent reliability analysis. The average river velocity model can be easily substituted by the maximal river flow velocity model when the corresponding statistical data are available.

According to the Manning–Strickler formula [22], given a site, the cross section average river flow velocity is governed by the following equation [23,24]:

$$v(t) = n^{-1} H(t)^{2/3} S^{1/2}$$
⁽¹⁾

where v(t) is the river flow velocity [m/s], n is the river bed roughness, H(t) is the hydraulic radius [m], and S is the river slope [m/m].

With the assumption that the shape of river bed is a rectangle, the hydraulic radius H is presented in terms of the depth (D [m]) and width (W [m]) of the river flow as follows:

$$H(t) = DW/(2D+W)$$
⁽²⁾

After carrying out research on a dataset of 674 river cross sections across the USA and Canada, Allen [25] found a relationship between the discharge, depth, and width with the following equations introduced by Leopold and Maddock [26]:

$$W = 2.71 d_m^{0.557} \tag{3}$$

and

$$D = 0.349d_m^{0.341} \tag{4}$$

where d_m is the discharge of the river [m³/s].

From above equations, given the river bed roughness and river bed slope, the river velocity is associated with the river discharge. Therefore, the statistical characteristics of the river flow velocity are governed by those of the river flow discharge.

2.1.2. Statistical characteristics of river flow velocity

Since the fluctuation of river flow discharge is much smaller than that of the wind speed, we use the monthly river flow discharge to describe the river flow discharge climate. The monthly river discharge follows a lognormal distribution [27–33]. Therefore, the cumulative probability density function (CDF) of the monthly river discharge is given by

$$F_{D_m}(d_m) = \Phi\{ \left[\ln(d_m) - \mu_{D_m}(t) \right] / \sigma_{D_m}(t) \}$$
(5)

in which $\mu_{D_m}(t)$ and $\sigma_{D_m}(t)$ are the mean and standard deviation of $\ln(d_m)$, respectively, $\Phi(\cdot)$ is the CDF of a standard normal variable. Due to the seasonality of the river discharge, $\mu_{D_m}(t)$ and $\sigma_{D_m}(t)$ are time-dependent, and they vary in different months during a year. The river discharge in the time domain is, therefore, a stochastic process. As illustrated in Fig. 1, the river discharge follows a certain statistical distribution at each time instant, and the mean, standard deviation of the distribution vary over time.

Besides, the monthly river discharge d_m at each time instant can be normalized and standardized [14,29,34–36]. The coefficient of autocorrelation of the normalized and standardized monthly river discharge is approximated by

$$\rho_V(t_1, t_2) = \exp\left\{-\left[(t_2 - t_1)/\xi\right]^2\right\}$$
(6)

where ξ is the correlation length. Thus, the normalized and standardized monthly river discharge is a Gaussian process with autocorrelation function in Eq. (6). The normalization and standardization of the monthly river discharge will be discussed later.

In the above analysis, the cut-out river flow velocity V_c is not considered. When the river velocity reaches the cut-out river flow velocity, the hydrokinetic turbine will shut down for a safety reason. With such a cut-out velocity, the upper tail of the lognormal distribution of the river discharge is truncated, and Eq. (5) becomes

a time interval [0,t] into *n* time instants and the simulated river velocities at these time instants were $v(t_i)$, $i = 1, 2, \dots, n$, the maximum velocity over the time interval [0,t] would be

$$v_{\max} = \max\{v(t_i), i = 1, 2, \dots, n\}$$
 (8)

Since the river velocity is a random variable at each time instant, the maximum velocity v_{max} is also a random variable with an unknown distribution. In addition to this, the longer is the time period [0,*t*], the higher is the v_{max} . Fig. 2 shows the simulated CDFs of the maximum velocities of the Missouri river over different time periods.

We see that the CDF curves of the maximum river velocities shift from left to right when the time period becomes longer. This implies that the hydrokinetic turbine blades have a higher probability of failure when the time interval becomes larger. For the timedependent reliability analysis over different time intervals, different CDFs of the maximum river velocity are required. As the distribution of river velocity is non-Gaussian and the loading of the turbine blade is a non-linear response of the river velocity, we do not have explicit expression for the extreme loading on the turbine blades. If the simulation methods are employed to get the extreme loading of the turbine blades, the computational cost may not be affordable. To improve the efficiency, we will introduce an efficient time-dependent reliability analysis method for the hydrokinetic turbine blades in Section 3.

$$F_{D_m}(d_m) = F_{V_d}(d_m) / F_{V_d}(d_C) = \Phi\{ \left[\ln(d_m) - \mu_{D_m}(t) \right] / \sigma_{D_m}(t) \} / \Phi\{ \left[\ln(d_C) - \mu_{D_m}(t) \right] / \sigma_{D_m}(t) \} \quad (0 < d_m < d_C)$$
(7)

where d_C is the river discharge corresponding to the cut-out river flow velocity V_c , $F_{D_m}(d_m)$ is the CDF of the monthly river discharge d_m .

After obtaining the CDF of the monthly river discharge, we can also find the CDF of the river flow velocity as indicated in Eq. (1). Thus, the statistical characteristics of the river flow velocity are available with Eqs. (1) through (7).

2.1.3. Maximum velocity of the river

Recall that the river discharge in the time domain is a stochastic process, the associated river velocity in the time domain is a stochastic process as well. For a stochastic process, we are interested in the extreme value of the process as it is directly related to the reliability of the hydrokinetic turbine blades. If we discretized



Fig. 1. Illustration of river discharge stochastic process.

In the following sections, we will discuss the relationship between the river velocity and the turbine blade loading response.

2.1.4. River flow velocity on the hydrokinetic turbine

For a horizontal hydrokinetic turbine, a diffuser, as shown in Fig. 3, is typically used to increase the flow velocity that enters the turbine.



Fig. 2. CDFs of the maximum flow velocities.



Fig. 3. The diffuser for the horizontal hydrokinetic turbine.

With the diffuser, the river velocity on the hydrokinetic turbine, v_h , turns out to be

 $v_h(t) = C_{\text{diffuser}} v(t) \tag{9}$

where C_{diffuser} is the velocity increasing coefficient of the diffuser. The value of C_{diffuser} is dependent on the geometry of the diffuser.

2.1.5. River flow velocity analysis when turbine blades are rotating

In the above analysis, the rotation of hydrokinetic turbine is not taken into consideration. When the hydrokinetic turbine is under operation, seen from the section of the turbine blade, the relative velocity v_r acting on the turbine blades should be a combination of the axial velocity and tangential velocity in the rotor plane [37]. The combination of velocities is shown in Fig. 4. The relative velocity acting on the turbine blade is given by

$$v_r(t) = \sqrt{\left[v_h(t)(1-a)\right]^2 + \left[\omega r(1+a')\right]^2}$$
(10)

in which

$$\omega = \lambda v_h(t)/R \tag{11}$$

where *a* is the axial induction factor, *a'* is the tangential induction factor, ω is the angular velocity of the rotor, *r* is the radial position of the control volume, λ is the tip speed ratio, and *R* is the radius of turbine blade. Besides, the optimal values of *a* and *a'* are related to the chords, twist angles, pitch of the blade, and $\omega r/V_h(t)$. *a* and *a'* can be obtained from the blade element momentum model [37], and Prandtl's and Glauert's corrections have been made for *a* and *a'* [38] in the blade element momentum codes.

2.2. Loading of hydrokinetic turbine blades

According to the blade element momentum theory, if the lift coefficient C_l and drag coefficient C_d are known, the lift and drag forces per length are given by [37]

$$L = \rho v_r(t)^2 c(r) C_l / 2 \tag{12}$$

$$D = \rho v_r(t)^2 c(r) C_d / 2 \tag{13}$$



Fig. 4. River flow velocity in the cross section of the turbine blade.

respectively, where ρ is the water density, and c(r) is the chord at radius r; C_l and C_d are associated with the local angle of attack. Then the force of river flow acting on the blade can be decomposed into two components P_T and P_N , which are normal and tangential to the rotor plane, respectively. These forces are depicted in Fig. 5.

The normal force results in the flapwise bending moment at the root of a blade, as shown in Fig. 6.

The normal force per length, denoted by $P_{N,r}$ at radius r, is given by [37]

$$P_{N,r}(t) = L\cos\gamma + D\sin\gamma$$

= $0.5\rho \Big((v_h(t)(1-a))^2 + (\omega r(1+a'))^2 \Big) (c(r)C_l\cos\gamma + c(r)C_d\sin\gamma)$ (14)

where γ is the flow angle, which is the summation of the local angle of attack θ_{AOA} and the local pitch θ . The local pitch θ is the combination of the pitch angle θ_p and twist angle $\theta_t(r)$ of the blade. The flow angle is determined by the following equation:

$$\tan \gamma = [(1-a)v_h(t)]/[(1+a')\omega r] = (1-a)R/[(1+a')\lambda r] \quad (15)$$

After obtaining the flow angle, we can calculate the angle of attack at radius r by

$$\theta_{\text{AOA}} = \gamma - \left(\theta_p + \theta_t(r)\right) \tag{16}$$







Fig. 6. Bending moment on the turbine blade.

Then with the angle of attack, C_l and C_d at radius r can be calculated according to the airfoil's characteristics.

From Eqs. (9), (14) and (15), we have

$$P_{N,r}(t) = 0.5\rho v^{2}(t) C_{\text{diffuser}}^{2} \left((1-a)^{2} + r^{2} \lambda^{2} (1+a')^{2} / R^{2} \right) \\ \times (c(r) C_{l} \cos \gamma + c(r) C_{d} \sin \gamma)$$
(17)

Let

$$C_{1}(r) = C_{\text{diffuser}}^{2} \left((1-a)^{2} + r^{2}\lambda^{2} (1+a')^{2} / R^{2} \right)$$
(18)

$$C_2(r) = (c(r)C_l\cos\gamma + c(r)C_d\sin\gamma)$$
(19)

$$M_{\text{flap}}(t) = \sum_{i=1}^{N-1} \left(\frac{1}{3} \left(\frac{P_{N,r_{i+1}}(t) - P_{N,r_i}(t)}{r_{i+1} - r_i} \right) \left(r_{i+1}^3 - r_i^3 \right) + \frac{1}{2} \left(\frac{P_{N,r_i}(t)r_{i+1} - P_{N,r_{i+1}}(t)r_i}{r_{i+1} - r_i} \right) \left(r_{i+1}^2 - r_i^2 \right) \right)$$
(22)

where M_{flap} is the flapwise bending moment, $r_{i+1} = r_{\text{root}} + (R - r_{\text{root}})i/N$, and r_{root} is the radius of the hub.

Substituting Eq. (21) into Eq. (22), we obtain the flapwise bending moment at the root of the blade

$$M_{\rm flap}(t) = 0.5\rho \left(2.71 d_m^{0.557} / \left(2 + 7.765 d_m^{0.216} \right) \right)^{4/3} SC_{\rm sum} / n^2$$
(23)

in which

$$C_{\text{sum}} = \sum_{i=1}^{N-1} \left(\left[C_1(r_{i+1}) C_2(r_{i+1}) - C_1(r_i) C_2(r_i) \right] / (r_{i+1} - r_i) \right) \left(r_{i+1}^3 - r_i^3 \right) / 3 \\ + \left[C_1(r_i) C_2(r_i) r_{i+1} - C_1(r_{i+1}) C_2(r_{i+1}) r_i \right] / (r_{i+1} - r_i) \left(r_{i+1}^2 - r_i^2 \right) / 2 \right)$$

With a fixed tip speed ratio λ , Eq. (17) is rewritten as

$$P_{N,r}(t) = 0.5\rho v^2(t)C_1(r)C_2(r)$$
(20)

Substituting Eqs. (1) through (4) into Eq. (20) yields

$$P_{N,r}(t) = 0.5\rho \left(2.71 d_m^{0.557} / \left(2 + 7.765 d_m^{0.216} \right) \right)^{4/3} SC_1(r) C_2(r) / n^2$$
(21)

In order to calculate the bending moment at the root of the blade, we divide the blade into N segments as shown in Fig. 7(a). The blade can be further simplified as shown in Fig. 7(b).

Based on the assumption of a linear variation of the load, the flapwise bending moment at the root of the blade can be computed by [37]



(a) Segments of the hydrokinetic turbine blade



(b) Simplified turbine blade loading model

Fig. 7. Normal forces on the hydrokinetic turbine blade.

2.3. Material resistance

Due to the variability of blade materials, their strength should be characterized by a certain probability distribution. Similar to the work on the reliability analysis of steel structure [39,40], we assume that the distribution of the yield strength, m_s , of the blade material, follows a normal distribution with mean μ_s and standard deviation σ_s ; namely $m_s \sim N(\mu_s, \sigma_s)$.

In order to compute the maximum bending moment that the material can resist at the root of the blade, we simplify the cross section of the turbine blade as shown in Fig. 8. As for a hydrokinetic turbine blade, a thin skin is glued on a box-like structure (the main structure) to define the geometry, as shown on the left of Fig. 8. Since the shape of the main structure is almost rectangular, we can simplify the cross section as a rectangle, as shown on the right of Fig. 8. Given the box-like structure, the error from the assumption of the rectangular cross section is acceptable for the root section.

The allowable bending moment can thus be obtained by

$$M_{\rm allow} = m_{\rm s}a_0b_0^2/4 \tag{25}$$

where a_0 and b_0 are the width and height of the blade after simplification, respectively. They are random variables due to the tolerance of manufacturing and clearance of assembly.

2.4. Limit-state function for turbine blade reliability analysis

For hydrokinetic turbine blades, the bending moment should not exceed the allowable bending moment in Eq. (25). Based on this, applying Eqs. (23) through (25), we define the limit-state function as follows:

$$g(\mathbf{X}, \mathbf{Y}(t), t) = M_{\text{flap}}(t) - M_{\text{allow}}(t)$$
(26)

where **X** is the vector of random variables, and **Y**(*t*) is the vector of stochastic processes. In this problem, $\mathbf{X} = \{a_0, b_0, m_s\}$ and **Y**(*t*) has only one element, which is the monthly discharge d_m . $M_{flap}(t)$ is the flapwise bending moment given in Eq. (23), and $M_{allow}(t)$ is the

(24)



Fig. 8. Simplified cross section of the hydrokinetic turbine blade.

allowable bending moment given in Eq. (25). When $g(\mathbf{X}, \mathbf{Y}(t), t) > 0$, a failure occurs.

3. Reliability analysis

For the reliability analysis of hydrokinetic turbine blades, we assume that the seasonal effects repeat in the same time periods of any year. This assumption is based on the fact that the Earth circulates around the Sun annually with the same seasonal effects. The yearly river climates, therefore, are independent with the same seasonality. The probability of failure during a *T*-year operation can be calculated as

$$p_f(T) = 1 - \left[1 - p_f(Y_e)\right]^T$$
 (27)

where $p_f(T)$ is the probability of failure during *T* years; $p_f(Y_e)$ is the yearly probability of failure.

Consequently, the yearly probability of failure of the turbine blade should be calculated first. Calculating $p_f(Y_e)$ requires time-dependent reliability analysis.

3.1. Time-dependent reliability analysis

3.1.1. Time-dependent reliability analysis with upcrossing rate

The above mentioned yearly probability of failure $p_f(Y_e)$ is defined over a time interval [0,*t*], where *t* is equal to one year. $p_f(Y_e)$ is a time-dependent probability of failure, and a general form of the time-dependent probability of failure over time period [t_0 , t_e] is defined as

$$p_f(t_0, t_e) = Pr\{Z(\tau) = g(\mathbf{X}, \mathbf{Y}(\tau), \tau) > e(\tau), \ \tau \in [t_0, t_e]\}$$
(28)

where t_0 is the initial time of operation, and t_e is the end point of the evaluated time period. $e(\cdot)$ is a time-dependent limit state, and $Pr\{\cdot\}$ stands for a probability.

With the integration of the Poisson assumption based upcrossing rate method and the First Order Reliability Method (FORM), $p_f(t_0,t_s)$ is calculated by [20,41]

$$p_f(t_0, t_s) = 1 - \left[1 - p_f(t_0)\right] \exp\left\{-\int_{t_0}^{t_s} v^+(t) dt\right\}$$
(29)

where $v^+(t)$ is the upcrossing rate at t, $p_f(t_0)$ is the instantaneous probability of failure at the initial time point t_0 . An instantaneous probability of failure $p_f(t)$ is the likelihood of failure at a particular time instant t and is calculated by

$$p_f(t) = Pr\{g(\mathbf{X}, \mathbf{Y}(t), t) > e(t)\}$$
(30)

The instantaneous probability of failure can be solved with FORM. The equation for solving the instantaneous probability of failure will be given in the next section. Once we have the upcrossing rate $v^+(t)$, the time-dependent probability of failure $p_f(t_0,t_s)$ can be calculated by integrating $v^+(t)$ over $[t_0,t_e]$.

Apparently, the key for calculating $p_f(t_0,t_s)$ with Eq. (29) is the computation of the upcrossing rate $v^+(t)$. In the following

subsections, we first review how to obtain the upcrossing rate by using FORM and the Rice's formula. We then discuss how to apply this method to the time-dependent reliability analysis of hydrokinetic turbine blades.

3.1.2. Upcrossing rate $v^+(t)$

For a general limit-state function $Z(t) = g(\mathbf{X}, \mathbf{Y}(t), t)$ given in Eq. (28), at a time instant t, its random variables and stochastic processes ($\mathbf{X}, \mathbf{Y}(t)$) are transformed into the standard normal random variables $\mathbf{U}(t) = (\mathbf{U}_{\mathbf{x}}, \mathbf{U}_{\mathbf{Y}}(t))$. After the transformation, the limit-state function is linearized at the Most Probable Point (MPP) $\mathbf{U}^*(t)$, which is a point at the limit state, and at this point the limit-state function has the highest probability density. Then at the MPP, the probability of failure is equivalent to

$$Pr\left\{L(t) = \boldsymbol{\alpha}(t)\mathbf{U}(t)^{T} > \boldsymbol{\beta}(t), \ t \in [t_{0}, t_{e}]\right\}$$
(31)

where

$$\boldsymbol{\alpha}(t) = \nabla \mathbf{g} \left(\mathbf{U}^{*}(t), t \right) / \left\| \nabla \mathbf{g} \left(\mathbf{U}^{*}(t), t \right) \right\|$$
(32)

 $\beta(t)$ is the reliability index, which is the length of $\mathbf{U}^*(t)$; and $\|\cdot\|$ stands for the length of a vector. Besides, the reliability index is used to calculate the instantaneous probability of failure at a time instant t_i as follows:

$$p_f(t_i) = 1 - \Phi(\beta(t_i)) \tag{33}$$

The above equation can also be used to calculate the initial instantaneous probability of failure $p_f(t_0)$ in Eq. (29).

From Eq. (32), we have $||\alpha(t)|| = 1$, and L(t) is therefore a standard normal stochastic process. Then the uncrossing rate $v^+(t)$ can be calculated using the Rice's formula [42,43] as follows:

$$v^{+}(t) = \omega(t)\phi(\beta(t))\Psi(\dot{\beta}(t)/\omega(t))$$
(34)

where $\Psi({\mbox{{\cdot}}})$ is a function defined by

$$\Psi(\mathbf{x}) = \phi(\mathbf{x}) - \mathbf{x}\Phi(-\mathbf{x}) \tag{35}$$

 $\omega^2(t)$ is given in terms of the correlation function $\rho(t_1,t_2)$ of L(t) as follows:

$$\omega^2(t) = \partial^2 \rho(t, t) / \partial t_1 \partial t_2 \tag{36}$$

Since L(t) is a standard normal stochastic process, its coefficient of correlation is given by

$$\rho(t_1, t_2) = \alpha(t_1) \mathbf{C}(t_1, t_2) \alpha(t_2)^T$$
(37)

where $C(t_1,t_2)$ is the covariance matrix of $L(t_1)$ and $L(t_2)$ and has the following form:

$$\mathbf{C}(t_1, t_2) = \begin{bmatrix} \mathbf{I}_{n \times n} & \mathbf{0} \\ \mathbf{0} & \mathbf{C}^{\mathsf{Y}}(t_1, t_2) \end{bmatrix}$$
(38)

where $\mathbf{I}_{n \times n}$ is an $n \times n$ identity matrix, which is the covariance matrix of the normalized random variables $\mathbf{U}_{\mathbf{x}}$ for \mathbf{X} , and $\mathbf{C}^{Y}(t_{1},t_{2})$ is the covariance matrix of the normalized stochastic process $\mathbf{U}_{\mathbf{Y}}(t)$. In

this problem, the covariance matrix just has one element, which is the covariance of the normalized river discharge stochastic process.

Given the correlation coefficients of the normalized stochastic process $\mathbf{U}_{\mathbf{Y}}(t)$, the covariance matrix $\mathbf{C}^{Y}(t_{1},t_{2})$ is presented as

$$\mathbf{C}^{Y}(t_{1},t_{2}) = \begin{bmatrix} C^{Y_{1}}(t_{1},t_{2}) & 0 & \cdots & 0\\ 0 & \ddots & \cdots & 0\\ \vdots & \vdots & \ddots & \vdots\\ 0 & 0 & \cdots & C^{Y_{m}}(t_{1},t_{2}) \end{bmatrix}$$
$$= \begin{bmatrix} \rho^{Y_{1}} & 0 & \cdots & 0\\ 0 & \ddots & \cdots & 0\\ \vdots & \vdots & \ddots & \vdots\\ 0 & 0 & \cdots & \rho^{Y_{m}} \end{bmatrix}$$
(39)

where $C^{Y_i}(t_1, t_2)$ is the covariance of the normalized stochastic process $U_{Y_i}(t)$ at time instants t_1 and t_2 . ρ^{Y_i} is the corresponding correlation function and is given by

$$\rho^{Y_i} = \rho^{Y_i}(t_1, t_2) \tag{40}$$

In this problem, the correlation of river discharge at two time instants can be obtained from Eq. (6).

Then substituting Eq. (37) into Eq. (36), we have

$$\omega(t)^{2} = \dot{\boldsymbol{\alpha}}(t)\dot{\boldsymbol{\alpha}}(t)^{T} + \boldsymbol{\alpha}(t)\ddot{\boldsymbol{\mathsf{C}}}_{12}(t,t)\boldsymbol{\alpha}(t)^{T}$$
(41)

in which

$$\ddot{\mathbf{C}}_{12}(t,t) = \begin{pmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \ddot{\mathbf{C}}_{12}^{Y}(t,t) \end{pmatrix}$$
(42)

and

$$C_{12}^{Y_i}(t,t) = \frac{\partial^2 \rho^{Y_i}(t,t)}{\partial t_1 \partial t_2}, \ i = 1, 2, \cdots, m$$
(43)

hydrokinetic turbine blades, we can then calculate its yearly probability of failure $p_f(Y_e)$ using Eqs. (29) through (45).

3.2. Time-dependent reliability analysis for hydrokinetic turbine blades

In this section, we use the time-dependent reliability analysis method presented above to solve for the probability of failure of hydrokinetic turbine blades. We first discuss the transformation of the non-Gaussian random variable (**X**,**Y**(*t*)) into standard Gaussian random variable **U**(*t*)=(**U**_{**x**},**U**_{**y**}(*t*)). Based on this, we then provide the approach of obtaining $\alpha(t)$ and $\beta(t)$ required by Eqs. (34) through (45) for time-dependent reliability analysis.

3.2.1. Transform non-Gaussian random variables

Due to the cut-out river flow velocity, a non-Gaussian random variable is involved. The non-Gaussian random variable is the truncated lognormal random variable (the truncated monthly river discharge). We need to transform it into equivalent normal distribution. The transformation is given by

$$U_{d_m} = \left[\ln(d_m) - \mu_{D_m}(t) \right] / \sigma_{D_m}(t) \sim N(0, 1)$$

$$(46)$$

where

$$\sigma_{D_m}(t)^2 = \ln\left[\left(\sigma_{d_m}(t)/\mu_{d_m}(t)\right)^2 + 1\right]$$
(47)

and

$$\mu_{D_m}(t) = \ln(\mu_{d_m}(t)) - 0.5\sigma_{D_m}(t)^2$$
(48)

After the truncation, the transformation becomes

$$\tilde{U}_{d_m} = \Phi^{-1} \left(\Phi \left[\ln(d_m) - \mu_{D_m}(t) \right] / \sigma_{D_m}(t) / \Phi \left[\ln(d_C) - \mu_{D_m}(t) \right] / \sigma_{D_m}(t) \right) (0 < d_m < d_C)$$

where *m* is the number of stochastic processes. For the turbine blade problem, m = 1.

 $\dot{\alpha}(t)$ and $\dot{\beta}(t)$ are required as indicated in Eq. (34) and Eq. (41). Because we use the finite difference method to calculate the derivatives, we need to carry out two MPP searches at every time instants *t* and *t* + Δt , where Δt is a small step size. The derivatives are given by

$$\dot{\boldsymbol{\alpha}}(t) = [\boldsymbol{\alpha}(t + \Delta t) - \boldsymbol{\alpha}(t)] / \Delta t \tag{44}$$

and

3.2.2. Solve for $\alpha(t)$ and $\beta(t)$

Recall that the limit-state function of the hydrokinetic turbine blade is

$$g(\mathbf{X}, \mathbf{Y}(t), t) = 0.5\rho \left(2.71 d_m^{0.557} / \left(2 + 7.765 d_m^{0.216}\right)\right)^{4/3} SC_{sum} / n^2 - m_s a_0 b_0^2 / 4$$
(50)

where C_{sum} is given in Eq. (24).

After the transformation, the limit-state function in Eq. (50) becomes

$$g(\mathbf{X}, \mathbf{Y}(t), t) = g(\mathbf{U}(t), t)$$

= $0.5\rho \left(2.71 \cdot T \left(\tilde{U}_{d_m} \right)^{0.557} / \left(2 + 7.765T \left(\tilde{U}_{d_m} \right)^{0.216} \right) \right)^{4/3} SC_{sum} / n^2 - 0.25T (U_{a_0}) T \left(U_{b_0} \right)^2 T (U_{m_s})$ (51)

$$\hat{\beta}(t) = [\beta(t + \Delta t) - \beta(t)]/\Delta t$$
(45)

Now all the equations are available for the upcrossing rate $v^+(t)$ in Eq. (29). If we know $\alpha(t)$ and $\beta(t)$ of the limit-state function of

where $T(\cdot)$ is the operator of transforming non-Gaussian random variables(**X**,**Y**(*t*)) into Gaussian random variables **U**(*t*).

Then, the MPP $\mathbf{U}^*(t)$ at a given time instant *t* can be obtained by solving

(49)

$$\begin{cases} \min \beta(t) = \|\mathbf{u}(t)\| \\ \text{s.t. } g(\mathbf{u}(t), t) = 0 \end{cases}$$
(52)

After obtaining the MPP $\mathbf{u}^*(t)$ at a given time instant *t*, we get $\alpha(t)$ and $\beta(t)$ as follows:

$$\beta(t) = \left\| \mathbf{U}^*(t) \right\| \tag{53}$$

and

$$\boldsymbol{\alpha}(t) = -\mathbf{U}^{*}(t) / \left\| \mathbf{U}^{*}(t) \right\|$$
(54)

Similarly, we can also solve for the $\alpha(t + \Delta t)$ and $\beta(t + \Delta t)$, which are then used to calculate $\dot{\alpha}(t)$ and $\dot{\beta}(t)$ in Eqs. (34) and (41). The yearly probability of failure $p_f(Y_e)$ is then solved with Eqs. (29) through (45). And the probability of failure during *T*-year operation, $p_f(T)$, is finally obtained with Eq. (27).

3.3. Sensitivity analysis of random variables

The time-dependent reliability analysis not only provides the likelihood of failure over a time period but also helps us understand how random variables affect such likelihood. The latter is achieved by sensitivity analysis. Sensitivity analysis shows the relative importance of each random variable to the probability of failure [44]. The sensitivities of random variables are represented by the sensitivity factors [45]. Since the limit-state function $g(\mathbf{X}, \mathbf{Y}, t)$ has been transformed into $g(\mathbf{U}, t)$, the sensitivity factor $\varepsilon_i(t)$ with respect to a random variable U_i (i = 1, 2, ..., 4) can be determined by

$$\varepsilon_{i}(t) = -\partial\beta(t)/\partial U_{i} = -\partial\left[\sum_{i=1}^{4} \left(U_{i}^{*}\right)^{2}\right]^{0.5} / \partial U_{i}^{*}$$

$$= -U_{i}^{*} / \left[\sum_{i=1}^{4} \left(U_{i}^{*}\right)^{2}\right]^{0.5} = -U_{i}^{*} / \beta(t)$$
(55)

Based on the sensitivity analysis of random variables at different instants of time, we can determine their importance on the failure of the turbine blade. Besides, the change of the importance of random variables over time period can also be evaluated. For important random variables identified by sensitivity analysis, we should focus on effective ways to quantify their uncertainties and identify their optimal distribution parameters during the design stage so that the probability of failure can be maintained at a desired level with a reduced cost.

4. Example

As mentioned previously, this work focuses on a hydrokinetic turbine with three 1-m long rotor blades, fixed pitch angle, and tip speed ratio, developed for the operation in the Missouri River. The sketch of the turbine is shown in Fig. 9. Its prototype under testing in a water tunnel is shown in Fig. 10. The reliability of the hydro-kinetic turbine over a 20-year design period was evaluated.

4.1. Data

The deterministic variables and distributions of the random variables are given in Tables 1 and 2, respectively. In order to calculate the parameters related to the geometry of the hydrokinetic turbine blade, we divided the blade into 30 segments. Assume that the turbine blade uses the NREL S809 airfoil section, which is shown in Fig. 11. The corresponding data of lift and drag coefficients were from [46]. The reason of using the NREL S809 airfoil for this example is that it has been widely studied by many researchers and



Fig. 9. 3-D modeling of a three blade hydrokinetic turbine.

that reliable lift and drag coefficients are available. The turbine blades are designed to have 1 m radius with non-linear chord length and twist angle distributions, which use the NREL S809 airfoil from root to tip. The optimized chord and twist angle distributions at different radii are plotted in Figs. 12 and 13, respectively. It is noted that the reliability analysis method in this paper can also handle other kinds of airfoil sections.

The historical river discharge data of the Missouri River from 1897 to 1988 at the Hermann, Missouri station [47] were used. Based on these data, we fitted the mean and standard deviation of the monthly river discharge as functions of t as follows:

$$\mu_{D_m}(t) = a_0^m + \sum_{i=1}^5 \left[a_i^m \cos(iw_m t) + b_i^m \sin(iw_m t) \right]$$
(56)

$$\sigma_{D_m}(t) = a_0^s + \sum_{j=1}^5 \left[a_j^s \cos(jw_s t) + b_j^s \sin(jw_s t) \right]$$
(57)



Fig. 10. A horizontal-axis hydrokinetic turbine with three blades under testing.

where

$$a_0^m = 2335, \ a_1^m = -1076, \ a_2^m = 241.3, \ a_3^m = 61.69, \ a_4^m = -30.92, \ a_5^m = 32.38, \ b_1^m = 57.49, \ b_2^m = -174.9, \ b_3^m = -296.2, \ b_4^m = 213.6, \ b_5^m = -133.6, \ \omega_m = 0.5583$$
 (58)

$$a_0^{\rm s} = 1280, \ a_1^{\rm s} = -497.2, \ a_2^{\rm s} = 145.8, \ a_3^{\rm s} = 225.4, \ a_4^{\rm s} = -203.1, \ a_5^{\rm s} = 99.47, \ b_1^{\rm s} = -82.58, \ b_2^{\rm s} = -19.06, \ b_3^{\rm s} = -178.7, \ b_4^{\rm s} = 36.15, \ b_5^{\rm s} = -52.47, \ \omega_{\rm s} = 0.5887$$

$$(59)$$

1/2

These functions were selected as the ones that give the best fits to measurement data available. Besides, according to the "over time" autocorrelation function of the Elbe River at Neu Darchau [29], the autocorrelation coefficient function of the monthly discharge of Missouri river is assumed to be

$$\rho_{D_m}(t_1, t_2) = \exp\left\{-\left[6(t_2 - t_1)/5\right]^2\right\}$$
(60)

4.2. Reliability analysis

By using the classical blade element momentum theory, the axial induction factor *a* and the tangential induction factor a' at different radii were computed first. Then the geometry related parameter C_{sum} was obtained from Eqs. (18), (19) and (24). After substituting the deterministic variables into Eq. (50), we obtained the limit-state function

$$g(\mathbf{X}, \mathbf{Y}(t), t) = 275.21 \left(2.71 d_m^{0.557} / \left(2 + 7.765 d_m^{0.216} \right) \right)^{4/3} - a_0 b_0^2 m_s / 4$$
(61)

The reliability analysis for the hydrokinetic turbine blade was conducted with the following steps: First, the probability of failure of the hydrokinetic turbine blades without a cut-out velocity in a one-year time period $[t_0,t_e] = [0,1]$ yr was analyzed by using the time-dependent reliability analysis method. Since the yearly probabilities of failure were assumed to be independent, then the probability of failure over the time life $[t_0,t_e] = [0,20]$ yr was computed using Eq. (27). Finally, in order to study the effect of cut-out velocity on reliability, we performed reliability analysis for the turbine blade with different cut-out river velocities. Meanwhile, as a byproduct of time-dependent reliability analysis, the sensitivities of random variables over time were also obtained.

Table 1

Table 2

Deterministic variables of the turbine blade problem.

Variable	ρ	λ	r _{root}	C _{diffuser}	V_C	θ	р	R	n	S
Value	$1 \times 10^3 \text{ kg/m}^3$	3	0.2 m	2	3.7 n	n/s 6	°	1 m	0.025	$4 imes 10^{-4} \text{ m/m}$

Distribution	of random	variables	of the	turhine	hlade	nrohler

Variable	Mean	Standard deviation	Distribution
d _m	$\mu_{d_m}(t)$	$\sigma_{d_m}(t)$	Lognormal
a_0	0.21 m	$1 \times 10^{-4} \text{ m}$	Normal
b_0	0.025 m	$1 \times 10^{-5} \text{ m}$	Normal
σ_s	$3.15 \times 10^5 \text{ kPa}$	$1.5 \times 10^4 \text{ kPa}$	Normal

4.3. Results and discussions

4.3.1. Time-dependent reliability analysis results

Table 3 shows the results of the probabilities of failure obtained from the time-dependent reliability analysis method. The solution from Monte Carlo Simulation (MCS) with a sample size of 1×10^6 are also presented in Table 3 and plotted in Fig. 14.

MCS is a simulation method, which can estimate the probability of failure accurately when the sample size is large enough. For the stochastic process (the monthly river flow discharge), we used the Expansion Optimal Linear Estimation method (EOLE) [48,49] to generate the samples for the river flow discharge.

The results indicate the good accuracy of the reliability analysis method for the hydrokinetic turbine blade presented. Fig. 14 and Table 3 show that the time-dependent probability of failure of hydrokinetic turbine blades increases with time over a one-year time period. The probability of failure is 2.546×10^{-4} over a one-year period after the hydrokinetic turbine is put into operation.







Fig. 12. Chords distribution along the radius of the turbine blade.



Fig. 13. Twist angle distribution along the radius of the turbine blade.

The probability of failure of the hydrokinetic turbine blades over its 20-year operation, or over $[t_0, t_e] = [0, 20]$ yr, is about 5.1×10^{-3} , which is obtained by substituting the yearly probability of failure 2.546×10^{-4} into Eq. (27).

4.3.2. Instantaneous probability of failure

We also calculated the instantaneous probability of failure. Fig. 15 shows such instantaneous probabilities and time-dependent probabilities of failure over different time periods in a one-year time period.

It is seen that the time-dependent probability of failure is much larger than its instantaneous counterparts after the third month. The instantaneous probability of failure does not increase with time while it fluctuates over time. There are several peaks in the curve of the instantaneous probability of failure. The reason is the seasonal characteristics of the Missouri River flow velocity. At these peak points, the river velocities are large. Besides, it can be found that an positive slope of the instantaneous probability curve will results in an increase in the time-dependent probability of failure.

4.3.3. Sensitivity analysis

As described in Sec.3.3, the sensitivity factors show the relative importance of each random variable to the probability of failure. Fig. 16 provides the sensitivity factors of the four random variables when there is no cut-out river flow velocity for the turbine.

The results indicate that the river velocity and the material strength make the highest contributions to the probability of failure and that the dimension variables of the cross section at the root of the turbine blade make negligible contributions. Besides, the

Table 3	
$p_f(t_0, t)$ of the hydrokinetic turbine blade over different time	period

Time period (months)	$p_f(t_0,t)$					
	Time-dependent $(\times 10^{-4})$	MCS solution $(\times 10^{-4})$				
[0, 1]	0.006	0.010				
[0, 2]	0.006	0.010				
[0, 3]	0.029	0.060				
[0, 4]	0.525	0.560				
[0, 5]	0.544	0.560				
[0, 6]	1.366	1.320				
[0, 7]	2.508	2.510				
[0, 8]	2.510	2.510				
[0, 9]	2.509	2.510				
[0, 10]	2.537	2.520				
[0, 11]	2.546	2.520				
[0, 12]	2.546	2.520				



Fig. 14. Probability of failure of the hydrokinetic turbine blade over different time intervals.

importance of random variables fluctuates with the time. The sensitivity factor of the material strength is positive, and this means that the probability of failure will decrease if the strength increases. On the contrary, the sensitivity factor of the river velocity is negative, and this indicates that the increase in the river velocity will result in the increase in the probability of failure. The river flow velocity is the most important contributor to the probability of failure of the hydrokinetic turbine blades. During the design stage, therefore, we should focus on the reduction of its effect on the reliability of the hydrokinetic turbine blades.

4.3.4. Influence of cut-out river flow velocity

4.3.4.1. Effect on the probability of failure. To study the effect of the cut-out river flow velocity, we performed reliability analysis with different levels of cut-out river flow velocities. Fig. 17 provides the results over a 20-year time life. By comparing the results without a cut-out river velocity, we see that a proper cut-out river velocity



Fig. 15. Instantaneous and time-dependent probability of failure.



Fig. 16. Sensitivity of random variables (without cut-out river velocity).

can decrease the risk of failure significantly. For example, the probability of failure over a 20-year operation with a cut-out velocity of 3.7 m/s is about 8.36×10^{-5} while its counterpart without a cut-out velocity is 5.1×10^{-3} . This indicates that the upper tail of the river velocity makes a great contribution to the probability of failure.

The selection of a proper cut-out velocity is therefore important. From Fig. 17, we see that when the cut-out velocity is high over the range from 4.15 m/s to 4.5 m/s, the change in the probability of failure will be slight with a reduced cut-out rive velocity. When the cut-out velocity is between 3.7 m/s and 4.15 m/s, a reduced cut-out velocity can affect the probability of failure dramatically. Moreover, to determine the optimum cut-out river velocity, we should also consider the influence of the cut-out river velocity on the power output. If the cut-out river velocity is set to be very low, the reliability of the turbine blade will be high while the power output will be sacrificed. On the other hand, if the cut-out river velocity is very high, the reliability of the turbine may not be satisfied. This implies that the reliability analysis method developed in this paper can be integrated with the power output model and energy-cost model of



Fig. 17. Time-dependent probability of failure of hydrokinetic turbine blade.



Fig. 18. Sensitivity of important random variables at MPP with and without cut-out river velocity.

the hydrokinetic turbine system to identify the optimum cut-out river velocity for the hydrokinetic turbine system.

4.3.4.2. Effect on the sensitivity of random variables. To examine how the cut-out river velocity affects the sensitivity, we plot the sensitivity curves for the important variables with and without cut-out river velocity as shown in Fig. 18. These variables include the river flow velocity and material strength. A cut-out river velocity of 3.7 m/s was used for the analysis in Fig. 18.

As shown in the figure, with the cut-out river velocity, the sensitivity factor of the river flow velocity decreases while that of the material strength increases. This indicates that by implementing a cut-out river velocity, we can reduce the sensitivity of the probability of failure with respect to the river velocity.

5. Conclusions

Reliability is an important factor to be considered during the hydrokinetic turbine design. The turbine blade reliability plays a critical role in the overall reliability of the hydrokinetic turbine system. In this work, we developed a time-dependent reliability analysis model for the hydrokinetic turbine blades. The blade element momentum theory was used to establish the limit-state function. The results show that the model can effectively evaluate the reliability of the hydrokinetic turbine blade over a certain time period.

We analyzed both of the time-dependent reliability over a time period and instantaneous reliability at an instant of time. The results showed that the time-dependent probability of failure is much larger than the instantaneous ones. Sensitivity analysis revealed that the river flow velocity and material strength make the highest contributions to the probability of failure of the hydrokinetic turbine blade and that the sensitivity of the probability of failure with respect to the river flow velocity is the highest.

The analysis also showed that a cut-out velocity affects the reliability of the hydrokinetic turbine in the following two aspects: First, an appropriately selected cut-out river velocity can decrease the probability of failure of the blade significantly. Second, with a cut-out river velocity, the contribution of the river flow velocity to the probability of failure decreases.

The pitch angle and tip speed ratio are assumed to be constant in this paper. But these parameters could be random. The cut-out velocity may also fluctuate in the real operation of the hydrokinetic turbine. These uncertainties will be considered in our future research. Even if the time-dependent reliability analysis model developed in this paper is based on the simplified models (the blade element momentum theory), it can be applied to more advanced models, such as the CFD and FEM simulations. In this work, we did not consider the spatial variation of the river flow velocity. We only treated it as a stochastic process. Our future work will account for the spatial variation of the flow velocity, and we will then model the velocity as a time-dependent random field.

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